



**NATIONAL
SENIOR CERTIFICATE/
NASIONALE
SENIORSERTIFIKAAT**

GRADE/GRAAD 12

JUNE/JUNIE 2023

**MATHEMATICS P1 MARKING GUIDELINE/
WISKUNDE V1 NASIENRIGLYN**

MARKS/PUNTE: 150

106

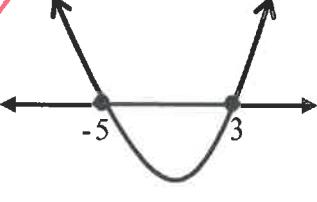
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NOTE/LET OP:

- If a candidate answered a question TWICE, mark the FIRST attempt ONLY.
Indien 'n kandidaat 'n vraag TWEE keer beantwoord het, merk SLEGS die EERSTE poging.
- Consistent accuracy(CA) applies in ALL aspects of the memorandum.
Volgehoue akkuraatheid geld deurgaans in ALLE aspekte van die memorandum.
- If a candidate crossed out an attempt of a question and did not redo the question, mark the crossed-out attempt.
Indien 'n kandidaat 'n poging vir 'n vraag deurgetrek het en nie die vraag weer beantwoord het nie, merk die poging wat deurgetrek is.
- The mark for substitution is awarded for substitution into the correct formula.
Die punt vir substitusie word vir substitusie in die korrekte formule toegeken.

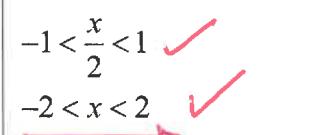
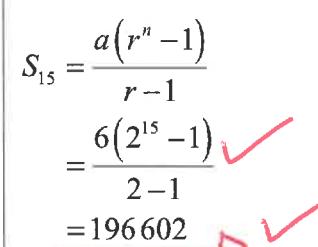
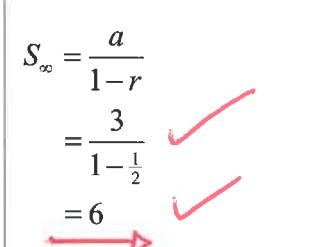
QUESTION 1/VRAAG 1

<p>1.1.1</p> $x^2 - 9 = 0$ $(x+3)(x-3) = 0$ $x+3 = 0 \text{ or/of } x-3 = 0$ $x = -3 \text{ or/of } x = 3$ <p>OR / OF</p> $x^2 - 9 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-(0) \pm \sqrt{(0)^2 - 4(1)(-9)}}{2(1)}$ $= \frac{\pm \sqrt{36}}{2}$ $x = -3 \text{ or/of } x = 3$	<p>OR / OF</p> $x^2 - 9 = 0$ $\checkmark x^2 = 9$ $x = \pm \sqrt{9}$ $\checkmark x = \pm 3$ <p>OR / OF</p> <p><i>ao 2/2</i></p> <div style="border: 1px solid black; padding: 5px; margin-top: 10px;"> Answers only – Full marks <i>Slegs antwoorde - Volpunte</i> </div>	<p>OR / OF</p> <p><i>✓ factors / faktore</i></p> <p><i>✓ both answers / beide antwoorde</i></p> <p><i>✓ correct substitution into correct formula / korrekte vervanging in korrekte formule</i></p> <p><i>✓ both answers / beide antwoorde</i></p> <p style="text-align: right;">(2)</p>
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1.1.2	$x - 5 + \frac{2}{x} = 0$ $x^2 - 5x + 2 = 0$ $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $x = \frac{-(5) \pm \sqrt{(-5)^2 - 4(1)(2)}}{2(1)}$ $x = \frac{5 \pm \sqrt{17}}{2}$ $\therefore x = 4,56 \text{ or/of } x = 0,44$	<p>Penalise 1 mark for incorrect rounding off. / Penaliseer 1 punt vir verkeerde afronding.</p> <p>$LCD = \infty (\because x \neq 0)$</p> <p>$x \neq 0$</p> <p>✓ standard form / standaardvorm</p> <p>✓ substitution / vervanging</p> <p>✓✓ x-values / waardes (4)</p>
1.1.3	$x = 1 + \sqrt{7-x}$ $x-1 = \sqrt{7-x}$ $(x-1)^2 = (\sqrt{7-x})^2$ $x^2 - 2x + 1 = 7 - x$ $x^2 - x - 6 = 0$ $(x+2)(x-3) = 0$ $\therefore x \neq -2 \text{ or/of } x = 3$	<p>✓ isolating surd / isoleer wortelvorm</p> <p>✓ square both sides / kwadreer beide kante ; check solutions!!!</p> <p>✓ standard form / standaardvorm</p> <p>✓ factors / faktore</p> <p>✓ selection / keuse (5)</p>
1.1.4	$x^2 + 2x - 15 \geq 0$ $(x+5)(x-3) \geq 0$ <p>critical values/kritieke waardes</p> $x = -5 \text{ or/of } x = 3$   <p>$x \leq -5 \text{ or/of } x \geq 3, x \in \mathbb{R}$</p> <p>OR/OF</p> $x \in (-\infty; -5] \text{ or/of } x \in [3; \infty), x \in \mathbb{R}$ <p>$\therefore x \leq -5 \text{ or } 3 \leq x$</p>	<p>✓ critical values / kritieke waardes</p> <p>✓✓ $x \leq -5 \text{ or/of } x \geq 3, x \in \mathbb{R}$ (accuracy / akkuraatheid) OR/OF</p> <p>$x \in (-\infty; -5] \text{ or/of } x \in [3; \infty), x \in \mathbb{R}$ (3)</p>

1.3 $\begin{aligned} & \sqrt[n]{\frac{10^n + 2^{n+2}}{5^{2n} + 4(5^n)}} \\ &= \left[\frac{2^n \times 5^n + 2^n \cdot 2^2}{5^n \cdot 5^n + 4(5^n)} \right]^{\frac{1}{n}} \\ &= \left[\frac{2^n(5^n + 4)}{5^n(5^n + 4)} \right]^{\frac{1}{n}} \\ &= \left[\left(\frac{2}{5} \right)^n \right]^{\frac{1}{n}} \\ &= \frac{2}{5} \end{aligned}$ <p style="text-align: right;">4</p>	$\checkmark \frac{2^n \times 5^n + 2^n \cdot 2^2}{5^n \cdot 5^n + 4(5^n)}$ \checkmark factors / faktore \checkmark changing surd to exponent / verandering van wortel na eksponent \checkmark answer / antwoord (4) [24]
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QUESTION 2/VRAAG 2

2.1.1	$r = \frac{T_3}{T_2} = \frac{6x}{12}$ $= \frac{x}{2}$ 	$\frac{12}{\cancel{24}} = 12 \times \frac{x}{\cancel{24}} = \frac{12}{1} \cdot \frac{x}{2}$ $= \frac{x}{2}$ <p>✓ answer / antwoord</p>	(1)
2.1.2	$-1 < r < 1$ $-1 < \frac{x}{2} < 1$ $-2 < x < 2$ 	 <p>✓ substitution / vervanging ✓ answer / antwoord</p>	(2)
2.1.3	$x = 4 \Rightarrow a = 6 \text{ & } r = 2$ $\checkmark a, r$ $S_{15} = \frac{a(r^n - 1)}{r - 1}$ $= \frac{6(2^{15} - 1)}{2 - 1}$ $= 196602$ 	 <p>✓ values of a and r / waardes van a en r ✓ substitution / vervanging ✓ answer / antwoord</p>	(3)
2.2	$T_1 = 6(2)^{-1} = 3$ $T_2 = 6(2)^{-2} = \frac{3}{2}$ $\therefore r = \frac{1}{2}$ $\checkmark a, r$ $3, \frac{1}{2}$ $S_\infty = \frac{a}{1-r}$ $= \frac{3}{1-\frac{1}{2}}$ $= 6$ 	 <p>✓ values of a and r / waardes van a en r ✓ substitution / vervanging ✓ answer / antwoord</p>	(3)

2.3.1	$S_{15} = -(15)^2 + 8(15)$ ✓ = -105 2	✓ substitution / vervanging ✓ answer / antwoord (2)
2.3.2	$T_{15} = S_{15} - S_{14}$ = -105 - (-84) ✓ = -21 2	✓ method / metode ✓ answer / antwoord (2)
2.3.3	$T_1 = S_1 = 7 = a$ $S_2 = -(2)^2 + 8(2) = 12$ OR / OF $7 + 14d = -21$ $\therefore T_2 = 5$ ✓ $\Rightarrow d = -2$ ✓ $a + (n-1)d = T_n$ $7 + (n-1)(-2) = -169$ ✓ ad T_n $7 - 2n + 2 = -169$ $-2n = -178$ $n = 89$ ✓ OR / OF 4	$a + 14d = -21$ $14d = -28$ $d = -2$ ✓ $T_2 = 5$ OR / OF $14d = -28$ ✓ $d = -2$ ✓ substitution / vervanging ✓ answer / antwoord OR / OF $S_n - S_{n-1} = T_n$ $-n^2 + 8n - [-(n-1)^2 + 8(n-1)] = -169$ $-n^2 + 8n - [-n^2 + 2n - 1 + 8n - 8] = -169$ $-n^2 + 8n + n^2 - 2n + 1 - 8n + 8 = -169$ $-2n = -178$ $n = 89$ ✓ formula / formule ✓ substitution / vervanging ✓ simplification / vereenvoudiging ✓ answer / antwoord (4) [17]

QUESTION 3/VRAAG 3

3.1	$95 ; 72 ; y ; 32 ; \dots$ $-23 ; y - 72 ; 32 - y ; \dots$ (first diff. / eerste verskille) $y - 49 ; -2y + 104$ $\therefore y - 49 = -2y + 104$ ✓ $3y = 153$ $y = 51$ ✓	2	✓ equating 2 nd differences / gelykstel van 2 ^{de} verskille ✓ answer / antwoord (2)
3.2	$95 ; 72 ; 51 ; 32$ $-23 ; -21 ; -19$ $2 ; 2$ $2a = 2$ ✓ $a = 1$ ✓ $3(1) + b = -23$ ✓ $b = -26$ ✓ $1 - 26 + c = 95$ ✓ $c = 120$ ✓ $T_n = n^2 - 26n + 120$ ✓	4	✓ 2 nd difference / 2 ^{de} verskil ✓ $a = 1$ ✓ $b = -26$ ✓ $c = 120$ (4)
3.3	$T_{22} = (22)^2 - 26(22) + 120$ $= 32$ ✓	1	✓ answer / antwoord (1)
3.4	$n^2 - 26n + 120 = 1040$ ✓ $n^2 - 26n - 920 = 0$ ✓ $(n - 46)(n + 20) = 0$ ✓ $n = 46$ or / of $n \neq -20$ ✓ OR / OF $n^2 - 26n + 120 = 1040$ $n^2 - 26n - 920 = 0$ $n = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ $= \frac{-(-26) \pm \sqrt{(-26)^2 - 4(1)(-920)}}{2(1)}$ $\therefore n = 46$ or / of $n \neq -20$	4	✓ equating / gelykstel ✓ standard form / standaardvorm ✓ factors / faktore ✓ answer / antwoord OR / OF ✓ equating / gelykstel ✓ standard form / standaardvorm ✓ substitution / vervanging ✓ answer / antwoord (4)
			[11]

QUESTION 4/VRAAG 4

4.1	$S(0;3)$	2	✓✓ answer / antwoord (2)
4.2.1	$x = -\frac{b}{2a} = -\frac{10}{2(-5)}$ ✓ $x = -1$ $T(-1; -2)$	4	✓ method / metode ✓ x-coordinate / x-koördinaat ✓ substitution / vervanging ✓ y-coordinate / y-koördinaat (4)
4.2.2	$p=1$ and / en $q=-2$	2	✓ $p=1$ ✓ $q=-2$ (2)
4.2.3	$\frac{5}{x+1} - 2 = 0$ ✓ $\therefore x = \frac{3}{2}$ $\Rightarrow \text{OR } = 1,5 \text{ units eenhede}$	2	✓ equating to 0 / stel gelyk aan 0 ✓ answer / antwoord (2)
4.2.4	$y \geq -2$ ✓ $y \in [-2; \infty)$	2	✓✓ answer / antwoord (2)
4.3.1	$m_{tan} = y' = 10x + 10 = 10(0) + 10 = 10$	2	✓ $m = 10$ ✓ substitution into eqn of line / vervanging in verg. van lyn ✓ answer / antwoord (3)
4.3.2	$y = (x+1)-2$ ✓ $y = x-1$ ✓ OR / OF	2	✓ substitution / vervanging ✓ answer / antwoord (2)
4.4	$x \geq \frac{3}{2}$		✓✓ answer / antwoord (A) (2)
			[19]

$$y = \frac{5}{x+p} + 2 \quad y = \frac{5}{x+1} - 2$$

AOS : $x+p = 0$
 $x = -p$ $x = -1$
 $-p = -1$
 $\therefore p = 1$

QUESTION 5/VRAAG 5

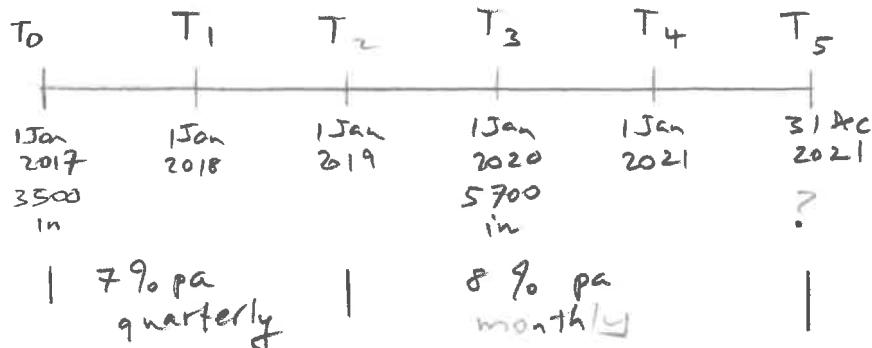
5.1	$h(x) = a^x$ $\frac{1}{2} = a^{-1}$ $\therefore a = 2$	Sub B(-1; $\frac{1}{2}$) $(\frac{1}{2})^{-1} = (a^{-1})^{-1}$ 2	✓ substitution / vervanging ✓ answer / antwoord (2)
5.2	$y = 2^x$ $x = 2^y$ $\therefore h^{-1}(x) : y = \log_2 x$	2	✓ interchanging x and y / omruil van x en y ✓ answer / antwoord (2)
5.3		4	✓ y-intercept for h / y -afsnit vir h ✓ shape and asymptote of h / vorm en asimptoot van h ✓ x-intercept for h^{-1} / x -afsnit vir h^{-1} ✓ shape and asymptote of h^{-1} / vorm en asimptoot van h^{-1} (4)
5.4	$x > 0$ → $x \in (0; \infty)$	1	✓ answer / antwoord (1)
5.5	$h^{-1}(x) > 1$ $y_{h^{-1}} > 1$ $x \in (2; \infty)$	$h^{-1}(x) = 1$ $\log_2 x = 1$ $2^1 = x$ $(2; 1)$	✓ answer / antwoord OR / OF ✓ answer / antwoord (1)
5.6.1	$t(x) = \left(\frac{1}{2}\right)^x - 1$ $= 2^{-x} - 1$	$h : y = (\frac{1}{2})^x$ $x \rightarrow -x$ $\downarrow -1$ 2	(2)
	✓ reflection about the <u>y-axis</u> / refleksie om die y -as ✓ shift of <u>1 unit down</u> / skuif van 1 eenheid af		✓ reflection / refleksie ✓ shift / skuif (2)
5.6.2	$y = -1$	1	✓ answer / antwoord (1)
			[13]

QUESTION 6/VRAAG 6

6.1	$A = P(1-i)^n$ $A = 980\ 000 \left(1 - \frac{9,2}{100}\right)^7$ $A = R498\ 685,82$	3	<ul style="list-style-type: none"> ✓ formula / formule ✓ substitution / vervanging ✓ answer / antwoord
6.2	$A = P(1+i)^n$ $20\ 020,28 = 13\ 500 \left(1 + \frac{8,2}{100}\right)^n$ $1,482\ 983\ 7037 = 1,082^n$ $\therefore n = \frac{\log 1,482 \dots}{\log 1,082}$ $n = 5 \text{ years/jaar}$	4	<ul style="list-style-type: none"> ✓ substitution / vervanging ✓ simplification / vereenvoudiging ✓ use of logs / gebruik van logs ✓ answer / antwoord
6.3	<p>Amount in savings account / Bedrag in spaarrekening :</p> $= 3500 \left(1 + \frac{7}{400}\right)^8 \left(1 + \frac{8}{1200}\right)^{36} + 5700 \left(1 + \frac{8}{1200}\right)^{24}$ $= R11\ 793,19$	OR / OF	<ul style="list-style-type: none"> ✓ $n = 8$ and / en $i = .7/400$ ✓ substitution / vervanging ✓ $n = 36$ and / en $i = 8/1200$ ✓ substitution / vervanging ✓ addition / optelling ✓ answer / antwoord
<i>show work</i>	$T_0 - T_2 \quad A_1 = 3500 \left(1 + \frac{7}{400}\right)^8 = R4\ 021,08624$ $T_2 - T_3 \quad A_2 = 4\ 021,08624 \left(1 + \frac{8}{1200}\right)^{12} = R4\ 354,834415$ $T_3 - T_5 \quad A_3 = 4\ 354,83441 + 5\ 700 = R10\ 054,834415$ <p>Final Amount / Finale Bedrag</p> $= 10\ 054,83441 \left(1 + \frac{8}{1200}\right)^{24}$ $= R11\ 793,19$	6	<p>OR / OF</p> <ul style="list-style-type: none"> ✓ $n = 8$ and / en $i = .7/400$ ✓ substitution / vervanging ✓ $n = 12$ and / en $i = 8/1200$ ✓ addition / optelling ✓ substitution / vervanging ✓ answer / antwoord

(6)

[13]



QUESTION 7/VRAAG 7

7.1

$$\begin{aligned}
 f'(x) &= \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h} \\
 &= \lim_{h \rightarrow 0} \frac{5 - 2(x+h)^2 - (5 - 2x^2)}{h} \\
 &= \lim_{h \rightarrow 0} \frac{5 - 2x^2 - 4xh - 2h^2 - 5 + 2x^2}{h} \\
 &= \lim_{h \rightarrow 0} \frac{-4xh - 2h^2}{h} \\
 &= \lim_{h \rightarrow 0} \frac{h(-4x - 2h)}{h} \\
 &= \lim_{h \rightarrow 0} (-4x - 2h) \\
 &= -4x
 \end{aligned}$$

Penalise 1 mark for incorrect notation in this question
 Penaliseer 1 punt vir verkeerde notasie in hierdie vraag

✓ $5 - 2x^2 - 4xh - 2h^2$

✓ simplification / vereenvoudiging

✓ factorisation / faktorisering (dividing by h / deel deur h)

✓ answer / antwoord

(4)

Answer ONLY: 0 marks
 SLEGS antwoord: 0 punte

7.2.1

$$\begin{aligned}
 f(x) &= 2x^5 - 7\sqrt{x} + \frac{1}{x} \\
 &= 2x^5 - 7x^{\frac{1}{2}} + x^{-1}
 \end{aligned}$$

✓ $2x^5 - 7x^{\frac{1}{2}} + x^{-1}$

✓ $10x^4$

✓ $-\frac{7}{2}x^{-\frac{1}{2}}$

✓ $-x^{-2}$

(4)

7.2.2

$$\begin{aligned}
 &\frac{d}{dx} \left[\frac{2x^2 - x - 6}{2x + 3} \right] \\
 &\frac{d}{dx} \left[\frac{(2x+3)(x-2)}{(2x+3)} \right] \\
 &\frac{d}{dx} [x-2] \\
 &= 1
 \end{aligned}$$

✓ factors / faktore

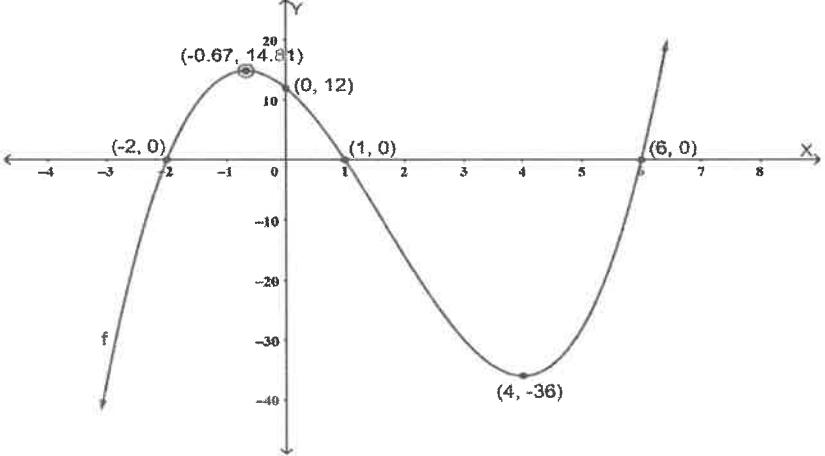
✓ simplification / vereenvoudiging

✓ answer / antwoord

(3)

[11]

20 || QUESTION 8/VRAAG 8

8.1	$f'(x) = 3x^2 - 10x - 8 = 0$ $(3x+2)(x-4) = 0$ $x = -\frac{2}{3}$ or / of $x = 4$ $y = \frac{400}{27} (14,81)$ or / of $y = -36$ $L\left(-\frac{2}{3}; \frac{400}{27}\right)$ and / en $M(4; -36)$	✓ $f'(x) = 0$ ✓ factors / faktore ✓ x-values / x-waardes ✓ y-values / y-waardes (4)
8.2	$f(x) = x^3 - 5x^2 - 8x + 12 = 0$ $(x-6)(x-1)(x+2) = 0$ $\therefore x = 6 ; x = 1 ; x = -2$	✓ factors / faktore ✓ $x = 1$ ✓ $x = -2$ (3)
8.3		✓ x-intercepts / x-afsnitte ✓ y-intercept / y-afsnit ✓ turning points / draaipunte ✓ shape / vorm (4)
8.4	$m = \frac{0 - (-16)}{6 - 2} = 4$ $y - y_1 = m(x - x_1)$ $y - 0 = 4(x - 6)$ $y = 4x - 24$ $\therefore a = 4$ and / en $q = -24$	✓ $a = 4$ ✓ $q = -24$ (2)
8.5	$f''(x) = 6x - 10$ $f''(2) = 6(2) - 10$ $= 2 > 0$ \Rightarrow concave up / konkaaf op	✓ $f''(x)$ ✓ substitution / vervanging ✓ conclusion / gevolgtrekking (3)
8.6	$4x - 24 = -36$ $x = -3$ $\therefore -3 \leq x \leq 2$ or / of $x \geq 6$	✓ equating / gelyk stel ✓ $x = -3$ ✓✓ answer / antwoord (4) [20]

08

QUESTION 9/VRAAG 9

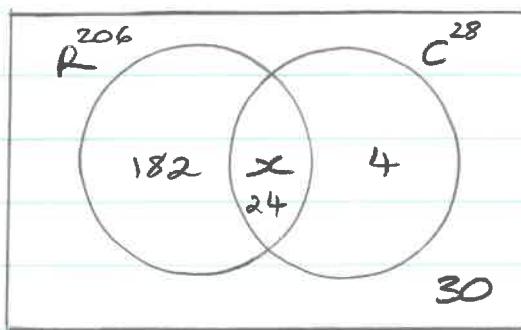
9.1	<p>Hourly cost = fuel cost + other costs <i>Uurlikse koste = brandstofkoste + ander koste</i> $= 4x^2 + 1000$</p> <p>Duration of trip/<i>Tydsduur van reis</i> = $\frac{\text{distance/afstand}}{\text{speed/spoed}} = \frac{500}{x}$</p> <p>Total cost/<i>Totale koste</i> $= (\text{hourly cost/uurlikse koste}) \times (\text{number of hours/aantal ure})$ $C(x) = (4x^2 + 1000) \times \left(\frac{500}{x}\right)$ $= 2000x + \frac{500\ 000}{x}$</p>	<p>✓ $4x^2 + 1000$</p> <p>✓ $\frac{500}{x}$</p> <p>✓ $(4x^2 + 1000) \times \left(\frac{500}{x}\right)$</p>	(3)
9.2	$C'(x) = 2000 - \frac{500\ 000}{x^2} = 0$ $2000x^2 - 500\ 000 = 0$ $2000x^2 = 500\ 000$ $x^2 = 250$ $x = \sqrt{250} = 15,81 \text{ km/h}$	<p>✓ $C'(x)$</p> <p>✓ $C'(x) = 0$</p> <p>✓ standard form / <i>standaardvorm</i></p> <p>✓ simplification / <i>vereenvoudiging</i></p> <p>✓ answer / <i>antwoord</i></p>	(5) [8]

QUESTION 10/VRAAG 10

10.1	$P(A \text{ or } / \text{ of } B) = P(A) + P(B)$ ✓ $0,64 = 3P(B) + P(B)$ ✓ $0,64 = 4P(B)$ $\therefore P(B) = 0,16$ ✓	$P(A \cap B) = 0$ mut excl	✓ rule / reël ✓ substitution / vervanging ✓ answer / antwoord	3
10.2.1	<pre> graph LR Start(()) --> Dry((Dry)) Start --> Wet((Wet)) Dry -- 37% --> FallDF((Fall)) Dry -- 88% --> NotFallDF((Not Fall)) Wet -- 63% --> FallWF((Fall)) Wet -- 36% --> NotFallWN((Not Fall)) </pre>	DF DN WF WN	✓ 37% and / en 63% ✓ 12% and / en 88% ✓ 36% and / en 64% ✓ outcomes / uitkomste	4
10.2.2	$P(F') = P(DF') + P(WF')$ $= \frac{37}{100} \times \frac{88}{100} + \frac{63}{100} \times \frac{64}{100} = \frac{7288}{10000} = \frac{911}{1250} = 0,73$		✓ $(37\% \times 88\%) + (63\% \times 64\%)$ ✓ answer / antwoord	2
10.3.1	$182 + x + 4 + 30 = 240$ OR / OF $x + 182 = 206$ OR / OF $x + 4 = 28$ $x = 240 - 216$ $x = 24$	$x = 24$ $x = 24$	✓ equation / vergelyking ✓ answer / antwoord	2
10.3.2	<p>For independent events <i>Vir onafhanklike gebeurtenisse</i></p> $P(R) \times P(C) = P(R \cap C)$ $P(R \text{ and } / \text{ en } C) = \frac{24}{240} = 0,10$ $P(R) \times P(C)$ $= \left(\frac{206}{240}\right) \times \left(\frac{28}{240}\right)$ $= 0,10$ <p>\therefore Yes, the events are independent. <i>Ja, die gebeurtenisse is onafhanklik.</i></p>		✓ $P(R \cap C) = 0,10$ ✓ $P(R) \times P(C) = 0,10$ ✓ conclusion / gevolgtrekking	3
			[14]	
			TOTAL/TOTAAL:	150

10.3. 1.

$$n = 240$$



2

$$\begin{aligned} 182 + x &= 206 \\ x &= 24 \end{aligned}$$

$$\textcircled{\text{OR}} \quad x + 4 = 28 \quad x = 24$$

$$\textcircled{\text{OR}} \quad 182 + x + 4 + 30 = 240 \quad x = 24$$

$$\begin{aligned} 10.3. 2. \quad P(R \cap C) &= \frac{24}{240} \\ &= \frac{1}{10} \\ &= 0,10 \checkmark \end{aligned}$$

$$\begin{aligned} P(R) \times P(C) &= \frac{206}{240} \times \frac{28}{240} \\ &= \frac{721}{7200} \\ &= 0,10 \checkmark \end{aligned}$$

\therefore to 2 dec places : NB see question!

$$P(R \cap C) = P(R) \times P(C)$$

\therefore Playing rugby and cricket are independent events

\therefore Yes \checkmark

3